

For an angle θ in standard position, with the terminal side intersecting the unit circle at the point (x, y) , the value of the secant function is given by $\sec \theta = \frac{1}{\cos \theta} = \frac{1}{x}$. Therefore:

$$\sec 45^\circ = \frac{1}{\frac{\sqrt{2}}{2}} = \frac{2}{\sqrt{2}} = \frac{2}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{2\sqrt{2}}{2} = \sqrt{2}$$