

When you attempted to eliminate variables you may have arrived at $0 = 0$ and interpreted the zeros to mean that there is no solution. However, there would be no solution for a system that leads to an *impossible* equation such as $0 = 1$.