The first inequality is false, but the second inequality is true. Because $e \approx 2.7$, it follows that $e < 3$, so $e^6 < 3^6$. The correct answer is $e^6 < 3^6 < 10^6$.