The first inequality is true, but the second inequality is false. Because $e\approx 2.7$, it follows that $e<3$ and $e<10$, so $e^6<10^6$. The correct answer is $e^6<3^6<10^6$.